

# Defining Yield Policies in a Viability Approach

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V European Conference on Ecological Modelling, 2005





- Study of the Southern Benguela ecosystem by Mullon



C. Mullon, P. Curry and L. Shannon

*Viability model of trophic interactions in marine ecosystems.*

*Natural Resource Modeling, 17:27-58, 2004.*

- **Problem:** Given constant values of fisheries, how ensuring the persistence of the ecosystem ?
- **Solution:** Study the model in a viability perspective
- We focus here on the yield policies



- 1 Southern Benguela ecosystem
- 2 Viability theory
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# Southern Benguela ecosystem

## Description

- 5 groups

- Detritus
- Phytoplankton
- Zooplankton
- Pelagic Fish
- Demersal Fish

- Sustainable system: the biomass of each species must remain in a given interval

Demersal

Pelagic

Zooplankton

Phytoplankton

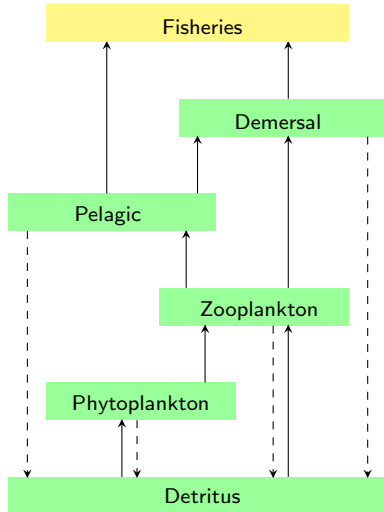
Detritus



# Southern Benguela ecosystem

## Model

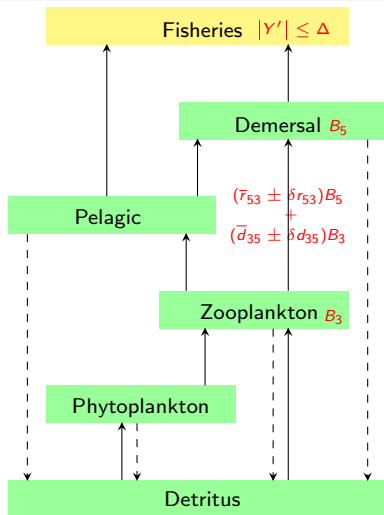
- Dynamical model of biomass evolution of each species, including
  - consumption
  - predation
  - yield
  - non-assimilated biomass (only for detritus)
- 6<sup>th</sup> compartment: fisheries



# Southern Benguela ecosystem

## Specifications of the model

- Thresholds for biomass  $m_i \leq B_i \leq M_i$
- Trophic flows fixed by the predator and the prey
- Thresholds for fisheries  $y_m \leq Y \leq y_M$
- Maximal variation  $|Y'| \leq \Delta$



# Southern Benguela ecosystem

## Specifications of the model



### Question:

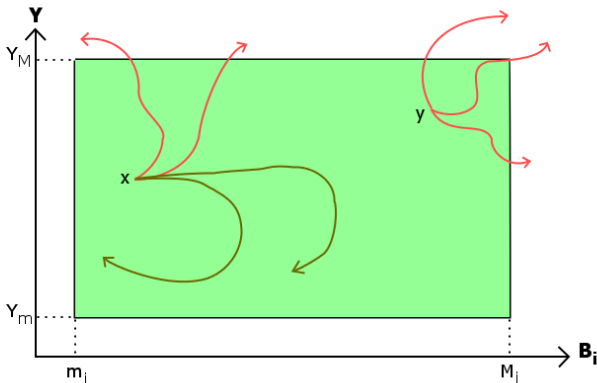
How define yield policies that allow the sustainability of the ecosystem ?



# Viability theory

## Definition

- **Viable state:** There exists at least one evolution which allows to stay in the viability constraint set

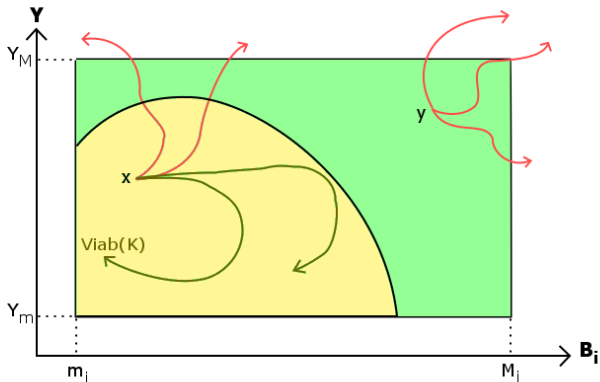




# Viability theory

## Definition

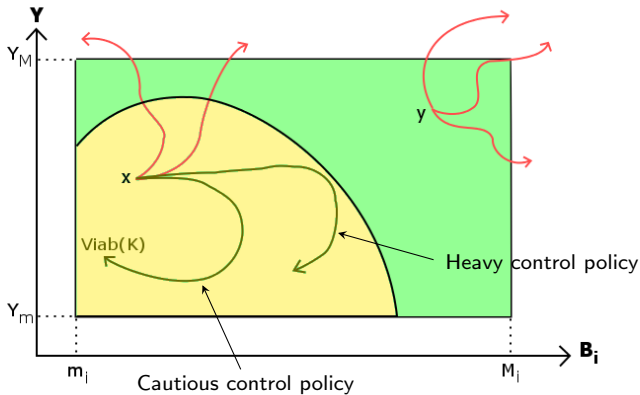
- Viability kernel: Set of all viable states




# Viability theory

## Definition

- Control policies: Flexibility for the stakeholders



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- 17 controls: trophic flows between species ( $\delta r_{ij}$ ,  $\delta d_{ij}$ ) and maximal variation of the yield ( $|Y'|$ )
  - Particular algorithm, based on a statistical learning method, Support Vector Machines, which approximates the viability kernel
  - Grid of 45000 points
  - Viability kernel: subset of  $R^6$



J.-P. Aubin

*Viability theory.*

Birkhauser, 1991.



P. Saint-Pierre

*Approximation of viability kernel.*

*Applied Mathematics & Optimisation*, 29:187-209, 1994.

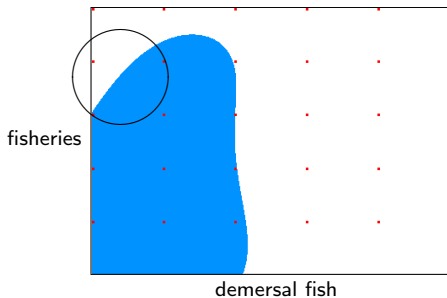


- A high level of detritus is necessary to ensure a viable path
- The levels of all the compartments have an influence on the boundary of the viability kernel
- Yield policies can be defined from the viability kernel

# Results

## Example of results I

- Low level of pelagic fish

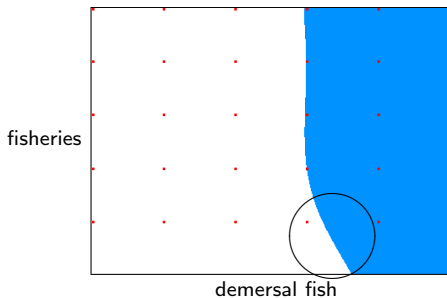


- maximal values of demersal fish
- maximal threshold for fisheries


# Results

## Example of results II

- High level of pelagic fish



- minimal values of demersal fish
- minimal threshold for fisheries

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- We focus on constraints on the ecosystem
  - Fisheries can be included in the problem.
  - Viability kernel helps to define yield policies

## Future work

- Other parameters to include ?
- Improve the accuracy of the results